

NOTES: CLASSIFYING AND MULTIPLYING POLYNOMIALS

What is a Polynomial?

An _____ of two or more algebraic _____.

$$\underline{3x^2} - \underline{5x} + \underline{2}$$

↑ ↑ ↑

Terms

Standard Form of a Polynomial

The standard form of a polynomial that contains one variable is written in alpha order with the terms in order from the _____ exponent to the _____ exponent. When written in **standard form**, the coefficient of the first term is the _____ coefficient.

Leading Coefficient → $4x^4 - 2x^3 + 3x^2 - x + 4$

Classifying Polynomials by Number of Terms

Number of Terms	Classification	Examples
1		$5x$
2		$2x + 7$
3		$5x^2 - 2x - 4$
4 or more		$3x^3 - 2x^2 - x + 4$

Some polynomials have special names based on their **degree** and the **number of terms** they have.

Classifying Polynomials by Degree

The **degree** of a polynomial is the polynomial degree of the term with the highest exponent.

3x⁴

↙

Degree	Classification	Examples
0	Constant	4
1	Linear	$7x$
2	Quadratic	$3x^2 + 1$
3	Cubic	$4x^3 - 2x^2 + 1$
4	Quartic	x^4

Rewrite each polynomial in standard form. Then classify by degree and number of terms.

1. $15 - 4x^2 + 2x^5$

Standard Form:

2. $20x - 4x^3 + 1 - x^2$

Standard Form:

Degree _____

Degree _____

Number of Terms _____

Number of Terms _____

3. $y^3 + y^4 - 3y$

Standard Form:

Degree _____

Degree _____

Number of Terms _____

Number of Terms _____

4. $1 + 3x$

Standard Form:

Degree _____

Degree _____

Number of Terms _____

Number of Terms _____

5. $-2x^2$

Standard Form:

Degree _____

Degree _____

Number of Terms _____

Number of Terms _____

Multiply and Monomial by a Polynomial

Recall your
Product Rule!
 $x^m \bullet x^n = x^{m+n}$

$2x^2(4x^4 - 3x^3 + 2x - 1)$

6. $6x(5x^2 - 10x)$

7. $-3m^2(-12m^2 - 8m + 5)$

8. $7x^3(5x^5 + 9x^2)$

9. $2ab^2(8a + 7b)$

10. $-\frac{1}{2}x^3y^2(10x^4 + 6x^3y - 2x^2y^4)$

11. $2x^7y(6x^5 + 5x^3y^2 - 3xy^4 - 1)$

A. CLASSIFYING AND MULTIPLYING POLYNOMIALS

Rewrite each polynomial in standard form. Then classify by degree and number of terms.

1. $6 - 3x^3 + x^4 + 7x$
Standard Form: _____

Degree _____

Number of Terms _____

2. $2x$
Standard Form: _____

Degree _____

Number of Terms _____

3. $3x + 4x^2 - 1$
Standard Form: _____

Degree _____

Number of Terms _____

4. $2x - 4x^3$
Standard Form: _____

Degree _____

Number of Terms _____

Multiply each monomial by the polynomial.

5. $5x^2(3x + 1)$

6. $3x^5(12x^2 - 2x - 5)$

7. $5xy^2(9x^2 - 4xy)$

8. $-6m^2n(-7m^4n^2 - 15m^2)$

9. $4m^3(3m + 7n^2)$

10. $2a^4b^2(5a^5b + 7a^3b^2 - 3ab + 4bc)$

11. $\frac{1}{2}x^4(12x^3 + 6x^2 - 8xy)$

12. $12x^3y(4x^2y + xy^2 - x - 1)$

13. $-2ab(5a^2b^2 + 21ab^2)$

14. $4x^2y^2(7x^2 - 8xy - 9xy^2)$

15. $xy^2(x^2y - x^2 + 4x + 2)$

16. $3x^3y^2(8x^3y^5 + 20x^2y^3)$