

# PROPERTIES OF OPERATIONS

Mathematical expressions can be written numerically, algebraically, and verbally. We can use the properties of operations to generate equivalent expressions.

## COMMUTATIVE PROPERTY

The commutative property allows you to change the order of the numbers without changing the solution. The commutative property only applies to \_\_\_\_\_ and \_\_\_\_\_.

### ADDITION

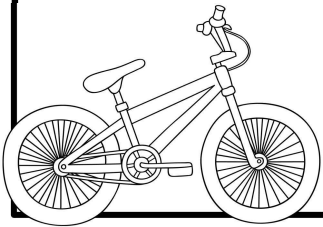
$$p + r + s = r + p + s$$

Prove it...if  $p = 12$ ,  $r = 5$ ,  $s = 2$

### MULTIPLICATION

$$p \cdot r = r \cdot p$$

Prove it...if  $p = 12$ ,  $r = 5$



a. Give an example to show why subtraction is NOT commutative.

## ASSOCIATIVE PROPERTY

The associative property allows you to group different sets of numbers together without changing the solution. The associative property only applies to \_\_\_\_\_ and \_\_\_\_\_.

### ADDITION

$$(p + r) + s = p + (r + s)$$

Prove it...if  $p = 12$ ,  $r = 5$ ,  $s = 2$

### MULTIPLICATION

$$(p \cdot r) \cdot s = p \cdot (r \cdot s)$$

Prove it...if  $p = 12$ ,  $r = 5$ ,  $s = 2$



b. Give an example to show why division is NOT associative.

## IDENTITY PROPERTY

The identity property allows a number to be added to or multiplied by \_\_\_\_\_ changing the number. The identity property only applies to \_\_\_\_\_ and \_\_\_\_\_.

### ADDITION

$$p + 0 = p$$

Prove it...if  $p = 12$

### MULTIPLICATION

$$p \cdot 1 = p$$

Prove it...if  $p = 12$

## INVERSE PROPERTY

When a number is multiplied or added to its inverse, it returns to its identity.

For addition, a number added to \_\_\_\_\_ will result in 0.

For multiplication, a number multiplied by \_\_\_\_\_ will result in 1.

### ADDITION

$$p + (-p) = 0$$

Prove it...if  $p = 12$

### MULTIPLICATION

$$\text{when } p \neq 0, p \cdot \frac{1}{p} = 1$$

Prove it...if  $p = 12$

Use your understanding of the properties of operations to complete 1-2.

1. For a-f, apply the given property to generate an equivalent expression or equation.

- $18 + q + 7 \rightarrow$  commutative property of addition  $\rightarrow$  \_\_\_\_\_
- $15 + b = 0 \rightarrow$  inverse property of addition  $\rightarrow$  \_\_\_\_\_
- $7 \cdot 8 \cdot 3 \rightarrow$  commutative property of multiplication  $\rightarrow$  \_\_\_\_\_
- $11 + 24 + 9 \rightarrow$  commutative property of addition  $\rightarrow$  \_\_\_\_\_
- $(6 + 5) + 8 \rightarrow$  associative property of addition  $\rightarrow$  \_\_\_\_\_
- $35(r) \rightarrow$  multiplicative identity property  $\rightarrow$  \_\_\_\_\_

2. Grady lists three different expressions below. Determine which expression is not equivalent to the others.

$$a + b + c$$

$$c + b + a$$

$$a(b) + a(c)$$

## PROPERTIES OF OPERATIONS

Answer the questions below. Be sure to show your work.

1. Which example shows the associative property of multiplication?

A.  $a(b + c) = ab + ac$

B.  $(a + b) + 9 = a(b + 9)$

C.  $(a \cdot b) \cdot 5 = a \cdot (b \cdot 5)$

D.  $(a \cdot b) \cdot 5 = (a \cdot \frac{1}{5}) \cdot b$

2. Which example does NOT show the commutative property of addition?

A.  $4 + x = x + 4$

B.  $ab = ba$

C.  $a + b = b + a$

D.  $3x + 4y = 4y + 3x$

3. Complete the table below to show an equivalent expression.

ORIGINAL EXPRESSION	PROPERTY	EQUIVALENT EXPRESSION
$15 + 0$	Additive Identity	
$4 \cdot 6 \cdot 7$	Commutative Property	
$9 + (5 + 3)$	Associative Property	
$11 \cdot 1$	Identity Property	
$\frac{1}{4} \cdot \frac{4}{1}$	Inverse Property	
$9 + (-9)$	Inverse Property	

4. Describe how you know that  $(8 + 9) + 3$  is equivalent to  $8 + (9 + 3)$ . What is the benefit to using this property?

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5. Describe how you know that  $9 + 7 + 1$  is equivalent to  $9 + 1 + 7$ . What is the benefit to using this property?

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