

# NOTES: SOLVE QUADRATICS BY Completing the Square

## The Goal of Completing the Square

To solve by completing the square, we will manipulate the equation to make it look something like this:

$$(x - 4)^2 = 25$$

Steps to solve:

1. Move \_\_\_\_\_ to right side of equation.
2. Add  $\left(\frac{b}{2}\right)^2$  to both sides of the equal sign, which will create a perfect square trinomial.
3. Factor the perfect square trinomial.
4. Take the \_\_\_\_\_ of both sides. Set up two equations and \_\_\_\_\_.

## When $a = 1$

1.  $x^2 + 6x - 40 = 0$

{ , }

2.  $x^2 + 10x + 9 = 0$

{ , }

When  $a \neq 1$

3.  $2x^2 + 28x - 30 = 0$

{ , }

4.  $2x^2 - 14x - 5 = 0$

When  $a = -1$

5.  $-x^2 - 8x + 20 = 0$

{ , }

6.  $-x^2 - 5x + 5 = 0$

# A. SOLVE QUADRATICS BY Completing the Square

Solve each quadratic equation by completing the square.

1.  $x^2 + 4x - 21 = 0$

2.  $x^2 + 2x - 63 = 0$

3.  $x^2 - 18x + 45 = 0$

4.  $x^2 + 4x - 5 = 0$

Scrambled answers:

$$x = \frac{-9 \pm \sqrt{101}}{2}$$

$$x = \{-15, -5\}$$

$$x = \{-2, 6\}$$

$$x = \{-10, 2\}$$

$$x = \{-5, 1\}$$

$$x = \{-9, 7\}$$

$$x = \{3, 15\}$$

$$x = \frac{-5 \pm \sqrt{33}}{4}$$

$$x = \{-4, 2\}$$

$$x = \{-7, 3\}$$

**5.**  $x^2 + 9x - 5 = 0$

**6.**  $2x^2 + 16x - 40 = 0$

**7.**  $3x^2 + 6x - 24 = 0$

**8.**  $2x^2 + 5x - 1 = 0$

**9.**  $-x^2 + 4x + 12 = 0$

**10.**  $-x^2 - 20x - 75 = 0$